



# How To Choose The Right Statistic Analysis Method

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# **Descriptive Statistics**

# Let's Start From the Basic

Different types of data:

- **Continuous**
  - Height, Weight, etc
- **Discrete**
  1. Binomial distribution
    - Infected vs. Non-infected, etc.
  2. Categorical
    - Nominal: Race, Color, etc
    - Ordinal: “On a scale from 1 to 5, how bad is your injury”, etc.
- **Time-event**
  - focusing on Time and Event at the same time
- **Count**
  - “How many times have you been infected with this disease”, etc

# Continuous

- ✓ Measures of Central Tendency
  - Mean
  - Median
  - Mode
  - Percentile
  - Range
- ✓ Measures of Differences
  - Variance
  - Standard Deviation
- ✓ Measures of Distribution
  - Symmetry
  - Skewness
  - Kurtosis
  - Usually use boxplot or histogram

# Discrete

- Frequency, proportion, percent
- table, pie charts, and bar charts



# **Statistical Analysis**

# Before you start your analysis...

1. What do you want to know
  - Correlation?
  - Discrepancy?
  - Independency?
2. What is your data type?
  - Continuous, discrete, etc.
3. How is your data distributed?
  - Normal distribution? Non-normal distribution?
4. How many variables do you have?
5. Is there a Dependent variable or an Independent variable?

## Here's an example

Assume we have 1000 gene expression samples from normal population, and 1000 gene expression samples from patients who were infected with an unknown disease.

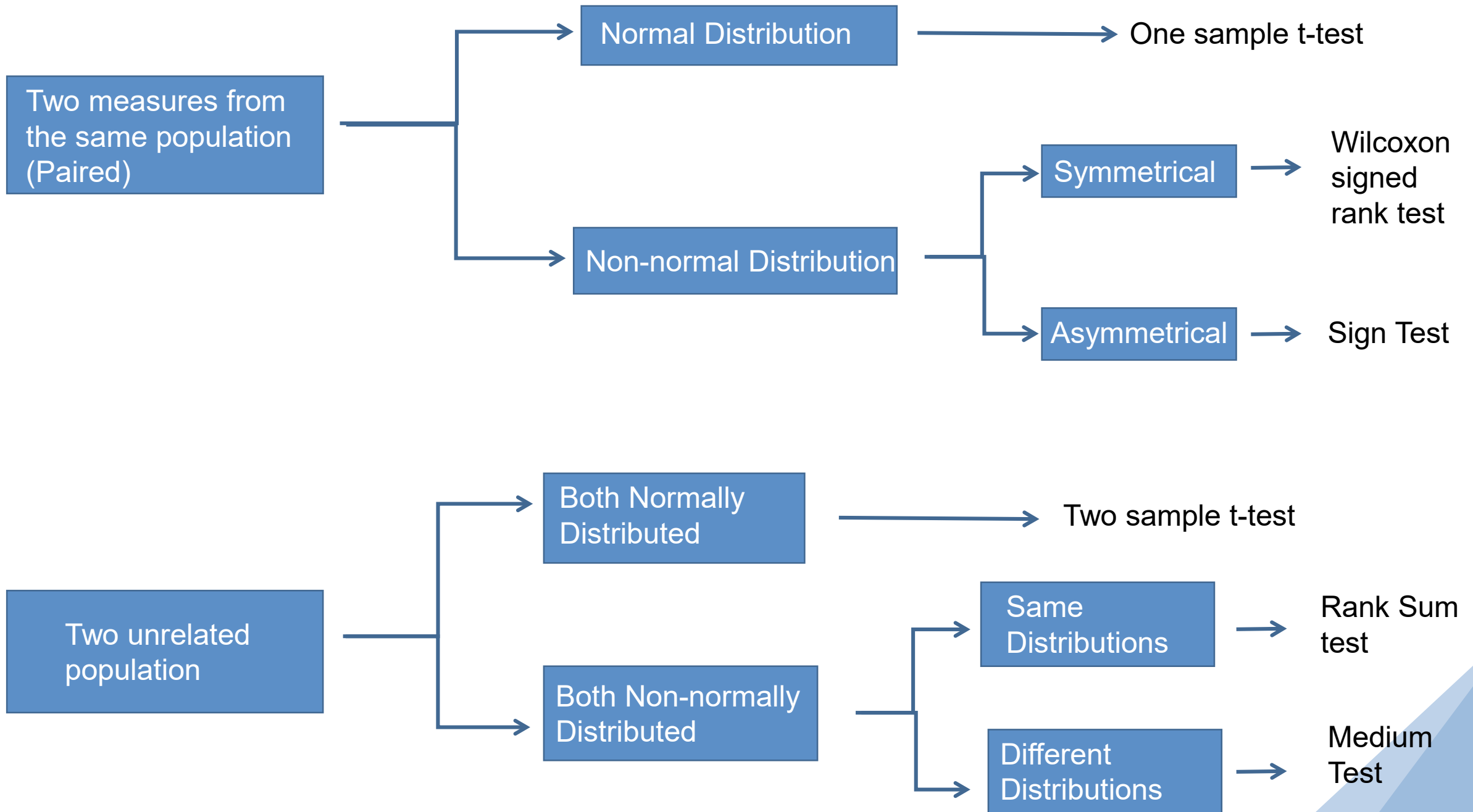
Question: Is there a significant difference between their gene expressions?  
What statistical analysis method do we use?

Do we use Two-sample t-test?

## Ask yourself these questions first...

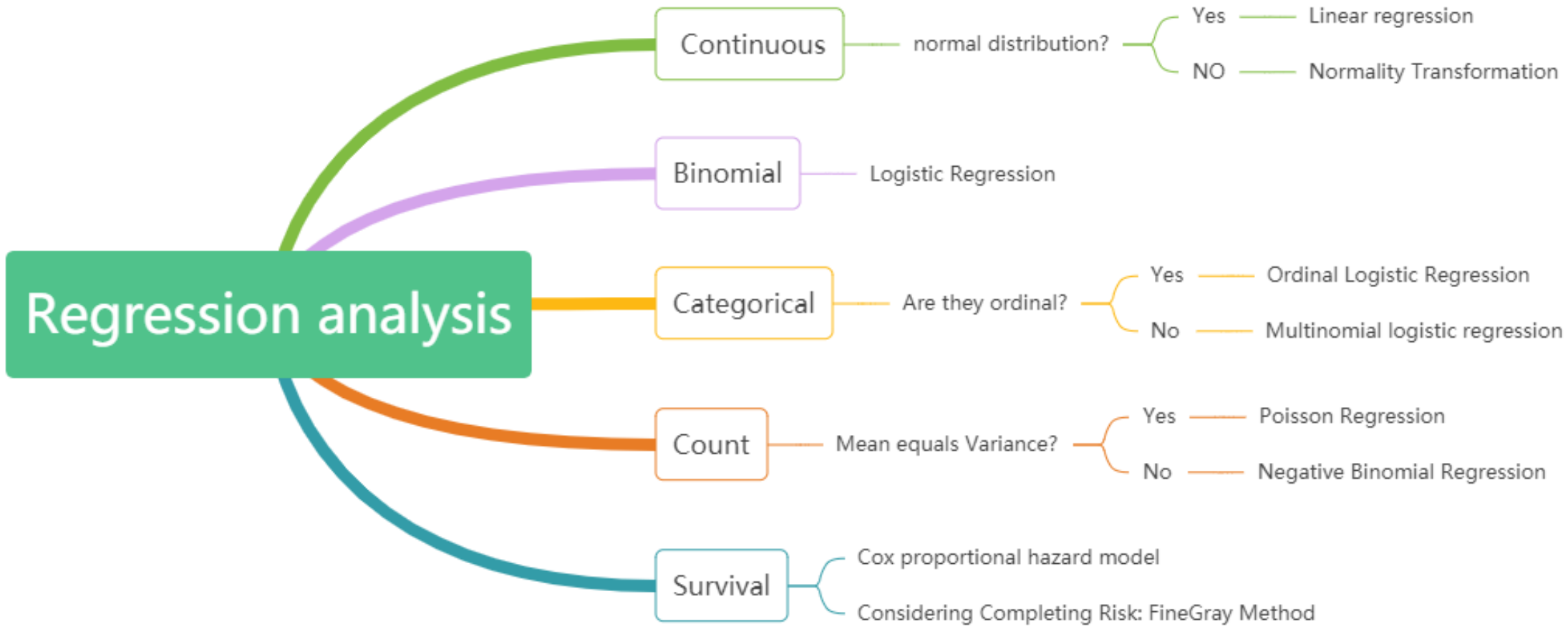
1. Is there any connections between “Normal population” and “Patient population”?
  - Gene expression from the same person? (Measured twice from the same population)
  - Are they related? Family members?(If yes, how do we deal with the data? And if not?)
2. How's the distribution of the data?
  - Normally distributed? Non-normally distributed?(How do you deal with them? )
3. Is there only two variables in this question?





1 \ 2	Continuous Normal distribution	Continuous Non-normal distribution	Binomial distribution	Nominal distribution	Ordinal distribution	Any type
Continuous Normal distribution	Pearson Correlation	Spearman correlation	t-test	Analysis of variance	Linear Regression	Linear Regression
Continuous Non-normal distribution		Spearman correlation	Wilcoxon rank test	Kruskal-Wallis test	Jonckheere-Terpstra test	Linear Regression
Binomial distribution			Chi-squared test	Chi-squared test	Cochran-Mantel-Haenszel test	Logistic Regression
Nominal distribution				Chi-squared test	Cochran-Mantel-Haenszel test	Multinomial Logistic Regression
Ordinal distribution					Cochran-Mantel-Haenszel test	Ordinal Logistic Regression
Time-event data						Kaplan-Meier Curve, Log-rank test

# If there're multiple variables...





# Sample Size

# What should we know about sample size calculation

- Things that will effect sample size:
  1. Significant level. (We usually pick 0.05)
  2. Power. (power =  $1-\beta$ )
  3. Effect size
- Common effect size: Risk Ratio(RR), Odds Ratio(OR), Hazard Ratio(HR)
- What if we do not have any of those, and still needs an effect size?
  - 1. Use effect size from previous related research (such as meta analysis)
  - 2. Perform a small sample size pre-research/pre-experiment to determine your effect size
  - 3. In 1988, Cohen mentioned in one of his research that effect size can be 0.2, 0.5, or 0.8 when you do not know the effect size for your experiment. 0.2, 0.5, and 0.8 represents small, medium, and large for your effect size. (Usually we choose 0.5)

For t-tests, the effect size is assessed as

$$d = \frac{|\mu_1 - \mu_2|}{\sigma}$$

where  $\mu_1$  = mean of group 1  
 $\mu_2$  = mean of group 2  
 $\sigma^2$  = common error variance

Cohen suggests that d values of 0.2, 0.5, and 0.8 represent small, medium, and large effect sizes respectively.

Sample size was estimated using data from previous tDCS studies,<sup>17,18</sup> antidepressant and rTMS meta-analyses,<sup>5,38,39</sup> and rTMS studies in which antidepressant drugs were combined.<sup>40,41</sup> With these data, we estimated a 3-point difference effect (effect size of Cohen  $d = 0.5$ ) for both tDCS only and sertraline only vs placebo and a combined additive effect in the combined treatment group (ie, 6-point difference, with an effect size of Cohen  $d = 1.0$ ), which, considering probabilities of 5% for type I error and 20% for type II error, resulted in an estimated sample size of 30 patients per arm for a total of 120 participants (for an extensive discussion regarding our power analysis, see the articles by Brunoni et al<sup>29,42</sup>). Further, we considered a difference smaller than an effect size of 0.5 or a 3-point between-group difference not to be clinically relevant per the National Institute for Clinical Excellence guidelines.<sup>43</sup>

# PASS

**Select a Procedure** Search Enter a Keyword

**Category** Favorites Recent Show All

- Design of Experiments
- Equivalence
- Group-Sequential
- Means
- One Mean
- Paired Means
- Two Independent Means**
- Two Means (Cluster-Randomized)
- Cross-Over (2x2) Design
- Cross-Over (Higher-Order) Design

**Confidence Intervals > Means (7)**

- Confidence Intervals for One Mean**
- Confidence Intervals for Mean with Tolerance P
- Confidence Intervals for Paired Means
- Confidence Intervals for the Difference Between Two Means
- Confidence Intervals for One-Way Repeated Measures Contrasts

**Means > Two Independent Means (42)**

- Two-Sample T-Tests Assuming Equal Variance**
- Two-Sample T-Tests Allowing Unequal Variance
- Two-Sample T-Tests using Effect Size
- Tests for Two Means (Simulation)
- Mann-Whitney-Wilcoxon Tests (Simulation)
- Tests for the Ratio of Two Means

**Select a Procedure** Search Enter a Keyword

**Category** Favorites Recent Show All

- Nonparametric
- Tools
- Microarray
- Non-Inferiority
- Nonparametric
- Normality
- Proportions
- One Proportion
- Two Correlated (Paired) Proportions
- Two Independent Proportions**
- Two Proportions (Cluster-Randomized)
- Contingency Table (Chi-Square Test)
- Repeated Measures

**Proportions > Two Independent Proportions (25)**

- Tests for Two Proportions
- Tests for Two Proportions using Effect Size
- Confidence Intervals for the Difference Between Two Proportions
- Confidence Intervals for the Ratio of Two Proportions

**Select a Procedure** Search Enter a Keyword

**Category** Favorites Recent Show All

- Logistic Regression
- Kappa Rater Agreement
- Sensitivity and Specificity
- Tools
- Quality Control
- Rates and Counts
- Regression
- ROC
- Simulation
- Superiority by a Margin
- Survival
- One Survival Curve
- Two Survival Curves**
- Cox Regression
- Exponential Means
- Confidence Intervals

**Survival > Two Survival Curves (16)**

- Logrank Tests
- Two-Group Survival Comparison Tests (Simulation)
- Tests for Two Survival Curves Using Cox's Proportional Hazards Model**
- Tests for the Difference of Two Hazard Rates Assuming an Exponential Model
- Logrank Tests Accounting for Competing Risks

**Select a Procedure** Search Enter a Keyword

**Category** Favorites Recent Show All

- Equivalence
- Group-Sequential
- Means
- Microarray
- Non-Inferiority
- Nonparametric
- Normality
- Proportions
- Quality Control
- Rates and Counts
- Regression
- Linear Regression
- Multiple Regression
- Cox Regression
- Poisson Regression
- Logistic Regression**
- Probit Analysis

**Regression > Logistic Regression (9)**

- Tests for the Odds Ratio in Logistic Regression with One Binary X (Wald Test)
- Tests for the Odds Ratio in Logistic Regression with Two Binary X's (Wald Test)
- Tests for the Interaction Odds Ratio in Logistic Regression with Two Binary X's (Wald Test)
- Confidence Intervals for the Odds Ratio in Logistic Regression with One Binary X
- Confidence Intervals for the Odds Ratio in Logistic Regression with Two Binary X's
- Confidence Intervals for the Interaction Odds Ratio in Logistic Regression with Two Binary X's
- Logistic Regression
- Tests for the Odds Ratio in a Matched Case-Control Design with a Binary X
- Tests for the Odds Ratio in a Matched Case-Control Design with a Quantitative X

**Calculate**

**Design**

Reports

Plots

Plot Text

**Design**

**Solve For:** Sample Size

**Test**

Alternative Hypothesis: Ha: Mean0 ≠ Mean1

Nonparam. Adj. (Wilcoxon Test): Ignore

Population Size: Infinite

**Power and Alpha**

Power: 0.90

Alpha: 0.05

**Effect Size**

**Means**

Mean0 (Null or Baseline): 0

Mean1 (Alternative): 1

**Standard Deviation**

S (Standard Deviation): 1

Known Standard Deviation

**Help Center**

For this procedure:

- Documentation
- Examples
- Validation
- Open Example Template

General:

- Getting Started Video
- Creating Power Curves Video
- All Training Videos
- Quick Start Documentation

**Option Info**

**Standard Deviation Estimator**

Click this button to load the standard deviation estimation tool.

Add This



- [-] Tests for One Mean
  - Numeric Results
  - References
  - Report Definitions
  - Summary Statements
  - Dropout-Inflated S
  - Procedure Input S

### Tests for One Mean

#### Numeric Results for One-Sample T-Test

Null Hypothesis: Mean0 = Mean1    Alternative Hypothesis: Mean0 ≠ Mean1  
 Unknown standard deviation.

Power	N	Alpha	Beta	Mean0	Mean1	S	Effect Size
0.91071	13	0.05000	0.08929	0.0	1.0	1.0	1.000

#### References

Machin, D., Campbell, M., Fayers, P., and Pinol, A. 1997. Sample Size Tables for Clinical Studies, 2nd Edition. Blackwell Science. Malden, MA.  
 Zar, Jerrold H. 1984. Biostatistical Analysis (Second Edition). Prentice-Hall. Englewood Cliffs, New Jersey.

#### Report Definitions

Power is the probability of rejecting a false null hypothesis. It should be close to one.  
 N is the size of the sample drawn from the population. To conserve resources, it should be small.  
 Alpha is the probability of rejecting a true null hypothesis. It should be small.  
 Beta is the probability of accepting a false null hypothesis. It should be small.  
 Mean0 is the value of the population mean under the null hypothesis. It is arbitrary.  
 Mean1 is the value of the population mean under the alternative hypothesis. It is relative to Mean0.  
 Sigma is the standard deviation of the population. It measures the variability in the population.  
 Effect Size,  $|\text{Mean0} - \text{Mean1}| / \text{Sigma}$ , is the relative magnitude of the effect under the alternative.

#### Summary Statements

A sample size of 13 achieves 91% power to detect a difference of -1.0 between the null hypothesis mean of 0.0 and the alternative hypothesis mean of 1.0 with an estimated standard deviation of 1.0 and with a significance level (alpha) of 0.05000 using a two-sided one-sample t-test.

The background features a white central area with blue wavy borders at the top and bottom. The top border consists of three overlapping, upward-curving bands in different shades of blue. The bottom border is a single, solid blue band that curves upwards from the bottom edge.

**Thank you**